CPT in Layered Soils and Correction of Thin-Layer Effect

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Abstract – CPT results (particularly the tip resistance, q_c) in a layered soil is affected not only by the properties of the layer in which the CPT cone in located, but also by layers ahead and behind the cone. In this study influence of sharp changes in the soil stiffness on q_c is analyzed through series of numerical simulations. The models contain one soft layer with thicknesses (h_s) vary from 50 to 300 mm, embedded in dense soil and with stiffness ratios (R_s , the ratio of the soft to dense soil stiffness) varying from 0.042 to 0.833. The transition zone (the distances above and below the soft layer in which the q_c is affected) were assessed as a function of h_s and R_s . Moreover, a correction method is proposed to back-calculate the actual q_c from the measured values.

Keywords: CPT, q_c , Layered Soils, Transition Zone, Thin-Layer Correction

1. Introduction

In many ground investigation projects, thin layers of soft soils embedded with relatively denser materials (or vice versa) are encountered. At or around the borders between the layer with different consistencies never can a sharp change in the cone penetration test (CPT) readings be observed, particularly in the cone tip resistance (q_c) . Influence of these thin layers can affect the results even when the CPT cone has still a remarkable distance to them. The affected zone (also named transition zone, TZ) can reach to 10-20 times cone diameter ([9]). [15] experimentally showed that q_c is influenced by the layers not only ahead of the CPT cone but also behind it.

[19] (NCEER) proposed a method for correction of CPT results in a denser soil interbedded between two softer layers in which the correction factor was a function of the dense layer thickness. [3] suggested that the transition zone corrections should not be uniformly applied over depth. Later [5] modified the method suggested in the NCEER by mathematically relating the correction factor to the shortest distance to the soft-to-dense boundary. That means the further from the denseto-soft boundaries the q_c is measured, the less impact has occurred, hence less correction would be needed. With numerical axisymmetric penetration studies on various combinations of two-layered soils, [2] showed that when entering from soft to dense soil, the border can be detected by CPT from a larger distance compared to when entering from dense to soft soil. They also stated that the cone senses the border farther ahead than behind. [4] introduced a so called Inverse Filtering, an iterative procedure, to estimate the unaffected q_c and sleeve friction (f_s) with sharp transitions. Several other researchers also investigated the CPT results in layered soils both experimentally (e.g., chamber test: [14][14], [10] and [6]; and centrifuge test: [11]) and numerically (e.g., cavity expansion: [12]; and axisymmetric penetration analysis: [18], [16] and [17]).

In this research series of models with one soft layer (with various thickness) embedded in dense soil were numerically simulated. The CPT cone selected in this work had diameter and tip angle of 35.7 mm and 60°, respectively. The Stiffness Ratio (R_s) (i.e., stiffness of soft soil (E_s) divided by that of the surrounding dense soil (E_d)) was another parameter whose sensitivity was studied over values from 0.042 to 0.833. Finally, the outcomes were discussed based on which a simplified correction method was introduced to estimate the actual (unaffected) q_c values.

2. Numerical Studies

2.1. Modelling CPT

Several studies have attempted to numerically model CPT (e.g., [8], [1], [13], [7] and many others). The most critical challenges that such modelling face are the complexity of the model due to the large deformations (mesh distortion) and the solution schemes (stress and deformation history in the soil, selecting an appropriate material model, interfaces, tension in soil, etc.).

Considering a continuous penetration of the CPT cone into the soil with a constant velocity (usually 20 mm/s) in the numerical modelling is a more realistic approach. However, regarding the complexity of situation, in this study a simplified method of modelling CPT was used, in which the cone does not penetrate throughout the depth in one run, but only 20 mm at consecutive and independent steps. First, the CPT cone and rod was modelled at a given depth. In the next phase of modelling, to simulate the penetration, a vertical displacement of 20 mm in one second was imposed on top of the rod. The mobilized vertical stress at top of the rod was considered as an indicator for the q_c . Then the CPT rod and cone was extended (re-modelled) to the next measurement level, the mesh was updated, and another 20 mm displacement was imposed. The same procedure was repeated to cover the whole investigation depth. The friction between CPT and soil was ignored and the CPT-to-soil interface could transfer only normal stress between the two bodies. The modelling was carried out using Plaxis 2D v.21.

This modelling approach fails to capture some aspects of the CPT test. In order to minimize the effect of the modelling limitations, the calculated vertical stress in the rod (here named σ_c) should not be considered directly as q_c , but can be normalized by a reference σ_c calculated in the same way. In section 3 the normalization procedure is explained.

2.2. Studied Conditions

In this study CPT test, with the above-mentioned modelling concept, was modelled in layered soils. The CPT cone was 35.7 mm in diameter and 60° in tip angle (one of most widely used cone types), and the ground consisted of a soft layer with various thicknesses embedded in a denser soil. Middle of the soft layer, however, was fixed in all models. The studied thicknesses of the soft layer were h_s = 50, 100, 200 and 300 mm. Depths of CPT penetration were selected so as to cover well above and below the soft later. Axisymmetric models with 250 mm width were developed to simulate the geometries as illustrated in Fig. 1.



Fig. 1: Geometry of the modelled conditions.

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The assigned soil model was Mohr-Coulomb for both soils. Moduli of elasticity of the soft and dense soils (E_s and E_d) as well as the stiffness ratio ($R_s = E_s/E_d$) are listed in Table 1. The assumed shear strength parameters were $\varphi'=32^\circ$ and c'=5 kPa for dense soil and $\varphi'=25^\circ$ and c'=10 kPa for soft soil (usually a silty soil), both with saturated and unsaturated density of 17 and 16 kN/m³. The material assigned to the CPT rod was linear elastic with modulus of elasticity of 200 GPa (modulus of elasticity of steel). A surcharge of 12.8 kPa represented an actual depth of 0.8 m for top of the model.

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E_s [MPa]	0.5	1	2	3	4	6	8	10
E _d [MPa]	12	12	12	12	12	12	12	12
R_s [-]	0.042	0.083	0.167	0.25	0.333	0.5	0.667	0.833

Table 1: Moduli of elasticity of the studied conditions.

3. Results and Discussions

3.1. Outcomes of Calculations

In this study the mobilized stress in the rod, denoted by σ_c (or calculated q_c) may not be 100% equal to the field q_c . The difference between σ_c and q_c lies within the modelling limitations. For example the lateral displacement of the soil due to downward penetration of the cone (which increases the stiffness in hardening soils) is missing. Another imperfection is not taking the stress history of the previous penetration steps into consideration. Moreover, the localized fractures occurring in the soil around an advancing CPT cone cannot be fully modelled in the FEM analysis. In order to minimize the modelling limitations, the calculated σ_c values of the layered soil were normalized by σ_c of the homogeneous condition (only dense soil).

In Fig. 2 the concept of normalization is presented. The calculated σ_c (with the assumptions mentioned in section 2) are presented in Fig. 2(a) for E_s of 2, 3, 4, 5 and 6 MPa and a constant value of 0.333 for R_s (i.e., $E_d = 6, 9, 12, 15$ and 18 MPa). In Fig. 2(b), σ_c values are normalized (hereafter named $\hat{\sigma}_c$) by dividing them by σ_c of dense soil with the corresponding E_d (same calculation procedure but without presence of the soft layer). Please note that in this graph, the zero depth is shifted to the center of the soft layer. As these analyses clearly show, the governing parameter affecting $\hat{\sigma}_c$ is R_s (the stiffness ratio). Changes in E_d and E_s have no influence on $\hat{\sigma}_c$ as long as R_s is fixed; that is the reason why in this research a constant value of 12 MPa for E_d was selected for all models, while R_s was ranging from 0.042 to 0.833.

In Fig. 3 $\hat{\sigma}_c$ values are plotted versus depth (zero depth at center of the soft layer) with four different soft layer thicknesses (h_s) and the moduli of elasticities as listed in Table 1. In some points there is minor unevenness in the results which are not expected in an idealized numerical simulation. This effect is due to influence of meshing quality on the results. As it can be seen in Fig. 1 the meshes' shape and size slightly differ from point to point where the tips of CPTs were modelled.

The lower R_s was, the larger drop was observed in the $\hat{\sigma}_c$. For h_s of 300 mm (and logically >300 mm) the $\hat{\sigma}_c$ reaches to an almost constant value in the soft soil. That means the Transition Zones (TZ, where the results were affected) inside the soft layer do not overlap for that thickness. In general, the extension of the TZ in the dense soil was larger than that in the soft soil (also stated by [2] and [15]). Regarding the results in the upper and lower dense soils, as also confirmed by other researchers (e.g., [2]), the TZ was wider in the upper dense soil compared to the lower one. Moreover, the extension of the TZ in the dense soil was a function of h_s and -as mentioned- R_s .



Fig. 2: (a) σ_c and (b) $\hat{\sigma}_c$ for $h_s=10$ cm and $R_s=0.333$ (E_s and E_d are given in the legend).



Fig. 3: $\hat{\sigma}_c$ for different soft layer thicknesses (h_s). $E_s=12$ MPa (h_s and E_s are given on the graphs).

Extension of the TZ can be visually identified and measured for different conditions. In Fig. 4(a) the TZ divided by the cone diameter (d_c =35.7 mm) is plotted against minimum $\hat{\sigma}_c$ ($\hat{\sigma}_{c,min}$). The TZ in the upper and lower dense soils are shown by green and white markers, respectively. Unlike R_s , $\hat{\sigma}_{c,min}$ is a parameter measurable from the results which can be correlated to R_s (see Fig. 2).

The upper and lower TZ seems to be a function of the $\hat{\sigma}_{c,min}$. The equations proposed based on the best fit are given on the graph (Eqs. 1 and 2). These formulas allow us to estimate the extend of TZ using the measured $\hat{\sigma}_{c,min}$. Dependency of TZ on h_s is less pronounced and can be ignored for the sake of simplicity.

In Fig. 4(b) $\hat{\sigma}_c$ values calculated at upper and lower limits of the soft soil (the black horizontal lines in Fig. 3) are drawn versus the $\hat{\sigma}_{c,min}$. Clearly there is no meaningful relation between the $\hat{\sigma}_c$ at the borders of soil layers and h_s , whereas a linear dependency to the $\hat{\sigma}_{c,min}$ can be observed with the equations suggested on the graph (Eqs. 3 and 4).



Fig. 4: (a) TZ in the upper and lower dense soils divided by d_c , (b) $\hat{\sigma}_c$ at upper and lower borders of soil layers, plotted against $\hat{\sigma}_{c,min}$ (h_s is given in the legend).

 T_{\cdot}

$$TZ/d_c = -7.27 \times \widehat{\sigma}_{c,min}^2 + 0.22 \times \widehat{\sigma}_{c,min} + 5.03$$
⁽¹⁾

$$Z/d_c = -5.02 \times \widehat{\sigma}_{c,min}^2 + 2.49 \times \widehat{\sigma}_{c,min} + 2.20$$
⁽²⁾

$$\hat{\sigma}_{c,upper} = 1.1 \times \hat{\sigma}_{c,min} + 0.2 \tag{3}$$

$$\hat{\sigma}_{c,lower} = 1.0 \times \hat{\sigma}_{c,min} + 0.1 \tag{4}$$

 $\hat{\sigma}_{c,min}$ value inside the soft layer was also found to be a function of h_s and R_s . For the sake of place, in Fig. 5 $\hat{\sigma}_c$ is presented only for two h_s and three R_s values. The solid curves show the measured $\hat{\sigma}_c$ (calculated in the layered soil) and the dotted lines are the actual $\hat{\sigma}_c$ (calculated in homogeneous soil either only soft or only dense, hence no thin-layer effect). As it can be seen, the thinner the soft layers is, the larger the difference between the measured and the actual $\hat{\sigma}_c$ in the soft layer will be. Dependency of this difference on h_s , however, is not consistent. The maximum difference took place where the $\hat{\sigma}_{c,min}$ was around 0.55, whereas, for larger and smaller $\hat{\sigma}_{c,min}$ values, the measured and actual $\hat{\sigma}_c$ in the soft layer were closer.

In Fig. 6(a) the actual and measured $\hat{\sigma}_{c,min}$ are compared. As mentioned, for large and small $\hat{\sigma}_{c,min}$, the measured and actual $\hat{\sigma}_{c,min}$ are almost on the 1-1 line, while in between the deviation is at its maximum. In Fig. 6(b) the markers show the difference between the measured and actual $\hat{\sigma}_{c,min}$ in the soft layer ($\Delta \hat{\sigma}_c$), and the straight lines simplify their trends.



Fig. 5: Measured and actual $\hat{\sigma}_c$ for h_s =50 and 100 mm (E_s and E_d are given in the legend).



Fig. 6: (a) actual $\hat{\sigma}_{c,min}$ and (b) $\Delta \hat{\sigma}_{c}$, plotted against measured $\hat{\sigma}_{c,min}$ (h_s is given in the legend).

3.2. Proposed Correction Procedure

In this paper a thin-layer correction method is proposed trying to back-calculate the actual q_c (unaffected by presence of an embedded soft layer) from the results measured on site. As mentioned earlier, in this study the calculated vertical stress in the CPT rod (σ_c) was considered as an indicator of q_c . σ_c was later normalized by σ_c of dense soil only, as a reference value. Likewise in a real CPT test done on such a ground (a soft layer embedded within denser soil), we can normalize q_c . Similar to the normalization concept of σ_c , the reference value for normalizing q_c could be the q_c before or after the cone senses the soft layer. Changes in the calculated and measured mobilized resistances in a CPT rod are expected to follow a similar trend. Therefore, \hat{q}_c (normalized q_c) and the $\hat{\sigma}_c$ are supposed to be in a same range and trend as both are normalized by their own quantities in the dense soil.

For real test results containing several soft and dense layers, the whole correction process should be repeated for every steep decrease or increase in q_c which is possibly an indication of presence of sharp soft/dense border. This method contains

two main steps: (1) identifying the soft/dense border affecting the CPT results, and (2) back-calculating the unaffected cone resistances in both soft and dense soils.

Step (1) where to apply the correction:

If \hat{q}_c drops to below 0.8 (i.e., more than 20% reduction in q_c) over a limited depth as estimated in Eq. (1), then this method could be deemed applicable.

For example if a reduction of 40% in q_c (i.e., $\hat{q}_c=0.6$) is recorded, it should have occurred over depth of $2.54 \times d_c \approx 90$ mm or less to consider a thin-layer correction for that. If this 40% drop has taken place over a thickness larger than 90 mm we can conclude that this reduction was not due to a sharp change in the soil stiffness, but as a result of a gradual transformation in the soil condition, hence no correction is needed.

Similar approach can be applied when an increase in q_c is recorded, but for this condition Eq. (2) may be used. For instance, in case 40% growth in q_c is observed (i.e., $\hat{q}_c=0.7$), it should be over a thickness of ~50 mm to consider this thin-layer correction.

Step (2) the proposed thin-layer correction:

Based on the findings of this study, the below procedure can be followed to back-calculate the unaffected and sharp q_c from the measured values:

1.Normalization of the tip resistance: $\hat{q}_c = q_c/q_{c,ref}$, where:

- In case of reduction in q_c : $q_{c,ref}$ is the tip resistance before the reduction starts

- In case on increase in q_c : $q_{c,ref}$ is the tip resistance after the increase finishes

2. Estimation of the measured \hat{q}_c at the actual depths of the soft/dense borders ($\hat{q}_{c,upper}$ and $\hat{q}_{c,lower}$) using equations Eqs. (3) and (4).

3. Estimation of the actual elevations of the soft/dense borders by locating the $\hat{q}_{c,upper}$ and $\hat{q}_{c,lower}$ values over the \hat{q}_c curve. The distance between these two points is the actual soft layer thickness (h_s) .

4. For outside the soft layer (i.e., the dense soil above and below), the measured q_c in the TZ can be corrected to $q_{c,ref}$ (see step 1).

5. Inside the soft layer, from the measured $\hat{q}_{c,min}$ and h_s (as estimated in step 3) we can estimate $\Delta \hat{q}_c$ using Fig. 6(b), and then calculate the actual \hat{q}_c (a constant value to be assigned over the h_s thickness):

actual
$$\hat{q}_c = measured \, \hat{q}_c - \Delta \hat{q}_c$$

- For $h_s>300$ mm the same measured $\hat{q}_{c,min}$ can be considered for the whole h_s thickness ($\Delta \hat{q}_c=0$).

4. Conclusions and Recommendations

From the outcomes of this study the following points can be concluded:

- CPT test can sense a soft layer located ahead of its cone from a larger distance than when it is behind.
- TZ is larger when CPT cone entered from a dense to a soft soil than the opposite order.
- As per the conducted analyses, the CPT results in layered soils (e.g., TZ shape, $\hat{q}_{c,min}$ or $\hat{\sigma}_{c,min}$) seem to be a function of stiffness ratio (R_s) rather than moduli of elasticity of the dense and soft soils individually.
- Extension of TZ in dense soils above and below a soft layer is more function of R_s than soft layer thickness (h_s) .
- For thin, soft layers (here <300 mm) the measured q_c inside the soft layer cannot reach to the actual (or unaffected) q_c values. This gap is found to be a function of R_s and h_s .
- A method is introduced in this paper to estimate the h_s and the actual q_c values inside and outside a soft layer embedded in dense soil from field data.
- The proposed correction procedure must be repeated for every sharp increase or decrease in q_c .
- In order to avoid human errors, this method is capable to be computerized.
- In a future research work, CPT tests can be conducted in layered soils with known parameters (e.g., calibration chamber test) to evaluate the proposed method.

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