

Topology Optimization of Heat and Mass Transfer Systems using Level-Sets and Anisotropic Mesh Adaptation

Wassim Abdel Nour¹, Joseph Jabbour², Damien Serret², Philippe Meliga¹, Elie Hachem¹

¹Mines Paris, PSL Research University, Centre de mise en forme des matériaux (CEMEF), CNRS UMR 7635
06904 Sophia Antipolis Cedex, France

wassim.abdel_nour@mines-paristech.fr, philippe.meliga@mines-paristech.fr, elie.hachem@mines-paristech.fr

²Temisth SAS

Technocentre "Henri-Fabre" - Technoparc des Florides - avenue Jacqueline Auriol - 13700 Marignane
joesph.jabbour@temisth.com, damien.serret@temisth.com

Extended Abstract

Keywords: Heat transfer, adjoint method, topology optimization, level-set method, anisotropic mesh adaptation

This study is devoted to the topology optimization of conjugate heat transfer systems governed by the coupled Navier-Stokes and heat equations. It is motivated by the need for performance improvement of the industrial heat exchangers used to regulate process temperatures, but thermal conditioning is of tremendous importance for a variety of applications ranging, for instance aircraft cabin climatization where the focus is on regulating in-cabin thermal conditions (temperature, humidity) under substantial variations of the ambient conditions to provide high-quality comfort for passengers.

Numerical experiments are performed using an in-house implementation of the variational multiscale stabilized finite element method [1]. The solid and fluid phases are represented on a single computational mesh with variable density, viscosity, conductivity, and specific heat. This removes the need for a heat transfer coefficient, as the amount of heat exchanged at the interface proceeds solely from the individual material properties on either side of it. The interface itself is described by level-set functions and is accurately discretized using anisotropic mesh adaptation to highly stretch the nearest cells [2]. Continuous adjoint problems are derived for cost functions typical of ducted flows [3]. Efficient enforcement of geometrical constraints (fixed/lower-bounded surface or volume) is achieved using not classical Lagrange multipliers, but a smooth Heaviside function that allows transporting the level-set (which in turn enlarges/shrinks the shape) when the current value strays too far away from the target.

For several cases involving competition between heat transfer enhancement and pressure drop reduction [4], this numerical framework has been found to yield accurate results while maintaining the CPU cost affordable. We will discuss the main results obtained in 2-D and 3-D, and will present novel optimal designs never documented in the literature, computed for extreme weights of the thermal objective.

References

- [1] E. Hachem, B. Rivaux, T. Kloczko, H. Digonnet, T. Coupez, Stabilized finite element method for incompressible flows with high Reynolds number, *Journal of Computational Physics*, Volume 229, Issue 23, 2010, Pages 8643-8665, ISSN 0021-9991, <https://doi.org/10.1016/j.jcp.2010.07.030>.
- [2] Coupez, Thierry & Hachem, Elie. (2013). Solution of high-Reynolds incompressible flow with stabilized finite element and adaptive anisotropic meshing. *Computer Methods in Applied Mechanics and Engineering*. 267. 65-85. 10.1016/j.cma.2013.08.004.
- [3] Othmer, Carsten. (2008). A continuous adjoint formulation for the computation of topological and surface sensitivities of ducted flows. *International Journal for Numerical Methods in Fluids*. 58. 861 - 877. 10.1002/flid.1770.
- [4] Subramaniam, V., Dbouk, T. And Harion, J.L. Topology optimization of conjugate heat transfer systems: A competition between heat transfer enhancement and pressure drop reduction. *Int. J. Heat Fluid Flow* (2019) 75: 165-184