

Unveiling the Flow Dynamics Spectrum: A Study of Corner Flow under No-Slip and Navier-Slip Condition

Ayelet Goldstein¹, Ofer Eyal²

^{1,2}Braude college of engineering
Post office Box 78 2161002, Karmiel, Israel
ayelet@braude.ac.il; ofer1eyal@gmail.com

Extended Abstract

In this study, we embark on a deep dive into the fascinating realm of laminar axial flow around a corner. Our investigation unfolds along two key axes: to scrutinize the intricate interplay between fluid dynamics and corner geometry, and to meticulously examine the impact of different boundary conditions (BCs) imposed at the fluid-solid interface.

We delve into two distinct BC scenarios: the "strict" no-slip condition [1,2,4], which dictates a stringent constraint of zero velocity at the solid surface, and the more "permissive" Navier's slip condition [2,3,5], which accommodates a degree of fluid slippage along the boundary.

Of particular interest is the delicate transition between these two scales of boundary behavior. Actualized by examples we show how a short distance theory smoothly becomes an effective at larger distances. Remarkably, we unveil a profound

analogy between the flow problem under investigation and the realm of stationary heat exchange. The heat exchange problem is one example of the possible application of our new method (combination of permitting BC and corner geometry) by use of one-one correspondence with a vast verity of natural problems [6-12], far beyond the confines of fluid dynamics.

References

- [1] A. Goldstein, O. Eyal, N. Brauner, and A. Ullmann, "Wall and interfacial shear stresses in laminar two-phase stratified flow in pipes," *Int. J. Multiphase Flow*, vol. 143, p. 103677, 2021.
- [2] O. Eyal, N. Brauner, A. Ullmann, and A. Goldstein, "Slip boundary condition near the wall-interface contact line in axial stratified two-phase flow," *Applied Mathematical Modeling*, 2023.
- [3] L. L. R. Pit, H. Hervet, "Direct experimental evidence of slip in hexadecane: solid interfaces," *Physical Review Letters*, vol. 85, pp. 980–983, 2000.
- [4] S. G. Y. Zhu, "Limits of the hydrodynamic no-slip boundary condition," *Physical Review Letters*, vol. 88, p. 106102, 2002.
- [5] D. R. W. V. S. Craig, C. Neto, "Shear-dependent boundary slip in an aqueous newtonian liquid," *Physical Review Letters*, vol. 87, p. 054504, 2001.
- [6] D. D. J. G. S. Beavers, "Boundary conditions at a naturally permeable wall," *Journal of Fluid Mechanics*, vol. 30, pp. 197–207, 1967.
- [7] C. D. M. D. C. Tretheway, "Apparent fluid slip at hydrophobic microchannel walls," *Physics of Fluids*, vol. 14, pp. L9–L12, 2002.
- [8] L. L. L. R. S. Voronov, D. V. Papavassiliou, "Review of fluid slip over superhydrophobic surfaces and its dependence on the contact angle," *Industrial and Engineering Chemistry Research*, vol. 47, pp. 2455–2477, 2008.
- [9] L. Dobrzynski and A. A. Maradudin, "Electrostatic edge modes in a dielectric wedge," *Physical Review B*, vol. 6, p. 972, 1972.
- [10] J. D. Jackson, *Classical Electrodynamics*. New York, NY: Wiley, 3 ed., 1999.
- [11] P. de Gennes, "Boundary effects in superconductors," *Rev. Mod. Phys.*, vol. 36, pp. 225–237, 1964.
- [12] J. Maxwell, "On stresses in rarefied gases arising from inequalities of temperature.," *Philos. T. Roy. Soc.*, vol. 170, pp. 231–256, 1879.