Rate-Dependent Cyclic Lateral Load Test on a Single Pile in Sand

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Abstract – The loading rate effect on a single pile subjected cyclic lateral loads is studied experimentally. The scaled model pile embedded in cohesionless sand is housed in a laminar shear box under 1g condition. Loads are applied with a horizontal actuator rigidly connected at the pile-head allowing only horizontal translation. The results show the significant effect of loading rate in bearing capacity of the lateral pile subjected to cyclic loading. Further, the variation of the lateral resistance of the pile are found to be linear function of logarithmic of the loading rate. However, no effect of loading rate appears in the bending moment, deflection and soil reaction profile along the pile depth, which indicates that soil near the pile show a consistent failure pattern despite a significant change in the loading velocity.

Keywords: single pile, cyclic load test, rate effect, model testing

1. Introduction

Single piles in coastal and offshore structures are inevitably subjected to repetitive lateral loads. Wind, waves, blasts, and water pressures may generate such cyclic lateral loads to the pile supported structures. These loads have wide range of amplitudes and velocities at different time events. Generally, all the cyclic loading sequences can be characterized by four parameters: a) the maximum applied load, b) the load variation amplitude, c) the number of cycles, and d) the loading rate. A number of studies have been conducted in the past considering first three parameters for the soil-pile system subjected to cyclic loading [1]–[4]. However, to the best of authors knowledge, the fourth parameter, i.e., the effect of loading rate on the cyclic lateral loads, has been neglected in most of the experimental investigations as well as analytical and numerical modelling.

In this study, a scaled single pile model embedded in dry homogeneous sand is investigated for lateral cyclic loading with wide range of loading rate and displacement amplitudes. The effect of loading rate on the failure pattern of the soil near the pile during are analysed in terms of load-deflection curve at the pile-head, bending moment distributions, pile deflections profile and soil reaction profile along the pile depth.

2. Model Test

Scaling of full-scale prototype to the fit in the laboratory test models are of fundamental importance for the simulation of actual behaviour of soil and structure material under reduced stresses, compared to the prototype. For the present experimental investigation, the scaling law derived by Kokusho and Iwatate [5] incorporating the effect of low confining pressure of soil pertaining to 1g condition was used. The similitude law considers the ratio of forces acting on the model and the prototype, suggesting a relationship between the model and prototype as,

$$\frac{\omega_m}{\omega_p} = \eta^{-1/4} \lambda^{-3/4}, \text{ and} \tag{1}$$

$$\frac{\gamma_m}{\gamma_p} = \eta^{1/2} \lambda^{1/2} \tag{2}$$

where, ω_m and ω_p are the cyclic loading frequency on the model and corresponding frequency on the prototype respectively, γ_m and γ_p are the dynamic strain on the model and corresponding strain on the prototype respectively, η is the density scaling ratio of the model to the prototype and λ is the geometric scaling ratio of the model to the prototype.

For the current experiment, η was adopted as 0.81 and λ was adopted 0.05. Physical dimensions and properties of the prototype and model used in this study are summarized in Table 1.

2.1. Experimental Setup

The experimental setup consists of a laminar shear box which is rigidly bolted with unidirectional shaking table owned by Saitama University, Japan. The base plate size of the shaking table is 1800 mm × 1800 mm with \pm 200 mm maximum stroke. The inside measurements of the shear box are 1200 mm in loading direction, 800 mm in perpendicular to the loading direction and 1000 mm in depth (Figure 1).

2.2. Sand

Dry, homogeneous and cohesionless Gifu sand found in Japan was employed in the experiment. The standard properties of the Gifu sand include the specific gravity 2.64 maximum diameter 0.84 mm, coefficient of uniformity 1.59, maximum and minimum void ratio 1.13 and 0.72, respectively. The friction angle of the Gifu sand is 40.7°.

The sand was put inside the shear box in seven successive layers and ach layer of sand was compacted with shaking table vibration of amplitude 7 m/s2 and frequency 40 Hz to get the desired density of soil (1.46 Mg/m^3). The corresponding void ratio was found to be 0.81 with an estimated relative density of 78%.

Items	Prototype	Model	Units
Length of pile (<i>L</i>)	18.0	0.9	m
Diameter of Pile (<i>d</i>)	0.8	0.04	m
Density of Pile (ρ_p)	2.4	1.5	Mg/m ³
Young's modulus of pile (E_p)	25.0	2.8	GPa
Depth of soil (<i>H</i>)	20.0	1.0	m
Density of soil (ρ_s)	1.8	1.46	Mg/m ³
Shear wave velocity (V_s)	171.5	96.0	m/s
Natural frequency of soil (f_n)	2.14	24.0	Hz

Table 1: Prototype to model relation

2.3. Pile

A solid cylindrical pile made of polyoxymethylene homopolymer (POM-H) with a diameter (d) = 40 mm and length (L) = 900 mm was used. A solid cubical POM-H pile-head (125 mm × 125 mm × 125 mm) was rigidly connected with the horizontal actuator providing restraints in movements except in the direction of loading. A vertical gap of 35 mm between the top surface of sand and pile cap was provided to eliminate the resistance of the pile cap. Figure 1(a) shows experimental setup of the single pile embedded in sand inside the shear box.

2.4. Pile instrumentation

19 pairs of strain gauges were applied over the length of the pile, as shown in Figure 1(b), to measure the induced bending strain in the loading direction. Strain gauges at shallow depth were placed at close spacing knowing the bending moments and displacements are confined to the pile depths immediately below the pile-head. The curvature is simply calculated by dividing the bending strain with the radius of the pile. Further, the moment (M) at depth z is calculated by multiplying the curvature with flexural rigidity (E_pI_p) of the pile. Finally, double differentiation and integration of the bending moment, as shown in Eqs. (3) - (4), provides an indirect estimate of soil resistance, p, and the lateral deflection of the pile, y, respectively;

$$p = \frac{d^2}{dz^2} M \tag{3}$$

$$y = \iint \frac{M}{E_p I_p} dz dz \tag{4}$$

Since the bending moment obtained from the experiment was a discrete data set, a continuous smooth data set was obtained from a data fitting. Various solutions for the data fitting and processing for a laterally loaded pile are available in in the literatures such as [5] and [6]. In this experiment, a polynomial equation method was used to process the experimentally experimentally measured bending strain data.



Fig. 1: Experimental setup detail (dimensions in mm): a) schematic diagram and b) strain gauge layout

2.5. Loadings

The loadings were applied at the pile-head using a digitally controlled unidirectional hydraulic actuator (± 10 kN, ± 150 mm). Four different displacement amplitudes of 5% of d (2 mm), 10% of d (4 mm), 15% of d (6 mm), and 20% of d (8mm) with three different loading rates of 0.01 mm/s, 10 mm/s and 250 mm/s were applied for consecutive 3 cycles. The soil was brought back to initial state after completing one loading rate case with all the displacement amplitude. The loading was applied in the ascending order of the loading amplitude for a selected loading rate case.

3. Results and Discussion

The force and pile-head deflection measured from the cyclic loading tests are shown in. Figure 2. The residual displacement in the force-displacement curve reveals the inelastic behaviour of the soil. However, the load deflection curve in the Figure do not show any yielding behaviour even with the large lateral deflection amplitude (20% of the pile diameter i.e., 8 mm). Similar results were reported in the monotonic lateral loading test on single pile by [8]. Degradation in the force in the successive cycles are clear in the loading part of the curve, whereas, unloading part is unaffected by the number of cycles.

Comparing the force-displacement diagrams in Figure 2. (a), Figure 2. (b) and Figure 2. (c) for 0.01 mm/s, 10 mm/s and 250 mm/s, respectively, the force increases with loading rate at any given displacements for both positive and negative cycles

of the loading. For example, at 8 mm displacement in the positive cycle, the increase in force with respect to 0.01 mm/s loading rate are 11% and 14% for 10 mm/s and 250 mm/s loading rate, respectively.



Fig. 2: Force-displacement relationship for: a) 0.01mm/s, b) 10 mm/s and c) 250 mm/s

A linear relationship between the force and loading rate is found as illustrated in Figure 3. This proves that the lateral resistance is approximately linearly proportional to the logarithmic of roading rate. The assumption was first proposed by [9] and used by other researches such as [10]. The equation of the fitted straight line in Figure 3 can be written as

$$F(v) = F(v_r) \left[1 - \alpha \log\left(\frac{v_r}{v}\right) \right]$$
(5)

Where, F(v) and $F(v_r)$ are the lateral resistance at a specific horizontal deflection at loading rates v and v_r, respectively; α is a coefficient defined as the increase in lateral resistance normalized by the lateral resistance at the reference loading rate. The α values for the positive cycle of loadings are summarized in Table 2.



Fig. 3: Force and loading rate in the positive cycle of loading for: a) 1st cycle, b) 2nd cycle and c) 3rd cycle

Displacements	2 mm	4 mm	6 mm	8 mm
1 st cycle	0.040	0.037	0.034	0.031
2 nd cycle	0.038	0.036	0.032	0.028
3 rd cycle	0.037	0.038	0.033	0.027

Table 2: Values of α at different displacement and different cycle

Moreover, bending moment profile along the pile length at various displacements ($\pm 2mm$, $\pm 4mm$, $\pm 6mm$ and $\pm 8mm$) with loading rate of 0.01 mm/s, 10 mm/s, and 250 mm/s are presented in Figure 4 (a), Figure 5 (a), and Figure 6(a), respectively, for successive 3 cycles. Out of 19 pairs of strain gauges, 3 pairs were damaged during the experiment, and therefore the data from remaining 16 pairs of strain gauges were utilized. Experimentally evaluated bending moments were fitted with a seven-degree polynomial equation. The fitted equation was further processed with double integration and double differentiation, as described earlier. The two boundary conditions employed during integrations are; a) known displacement at the pile-head, and b) an assumption of zero-degree rotation angle at the pile toe.

In contrast the to the rate dependency on the force-displacement behaviour, the bending moment, displacement and soil reaction profile are similar for different loading rates. This suggests the failure pattern of soil near the pile soil are consistent regardless of the rate of cyclic loading. Moreover, there is no effect of number of cycles on the bending moment, displacement and soil reaction profile of the soil-pile system.



a) b) c) Fig. 4: a) Bending moment, b) lateral deflection and c) soil reaction profile for 0.01 mm/s loading



Fig. 5: a) Bending moment, b) lateral deflection and c) soil reaction profile for 10 mm/s loading



Fig. 6: a) Bending moment, b) lateral deflection and c) soil reaction profile for 250 mm/s loading

4. Conclusion

The rate effect in cyclic loads to an instrumented pile model embedded in dry homogeneous sand is investigated experimentally under 1g condition. Wide range of velocities are applied with various displacement amplitude at the pilehead fixed in rotational direction. The loading rate effect is analysed on force-displacement relationship and bending moment, deflection and soil reaction profile over the length of the pile. Based on the results, it is concluded that the lateral bearing capacity of the pile subjected to cyclic loading significantly exhibits rate dependent characteristics. The rate dependent behaviour of bearing capacity can be approximated with a linear function of logarithmic of loading rate. However, the failure pattern of the soil near the pile is considered as a consistent behaviour. These findings provide valuable understanding of the laterally loaded pile under cyclic loading, which may help engineers to evaluate performance of the pile foundation more precisely.

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