

# Modelling Local Nusselt Numbers for Channels with Flow in Transition

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## Extended Abstract

This work reports a study of heat transfer in turbulent flow entering into small channels, which causes a transition to laminar flow. Heat transfer in channels has been extensively studied, especially the Nusselt-Graetz problem, most commonly constant wall temperature or constant wall heat flux. Early works reported Nusselt values for circular pipes with laminar developed flows, including analytical solutions validated with experiments. Later, developing laminar flows were also studied, presenting correlations for Nusselt-Graetz along the entry region. Most of the engineering flows are turbulent, in such flows, convection increases significantly and laminar flow assumptions are not valid. Although that there are Nusselt numbers reported for the developed turbulent flows, describing the entry region is still a challenge. In literature, flows in circular channels are classified into three main categories: Laminar for  $Re < 2300$ , turbulent for  $Re > 10000$ , and transitional for the  $Re$  in between [1]. However, some cases, such as monolith type substrates, fit into none of those categories. Monolith based reactors are extensively used in the automotive industry, since they produce lower pressure drop than fixed beds; they are implemented in several other industrial processes as well. It creates a growing interest in its modelling [2, 3]. Usually, the flow before a monolith is turbulent ( $Re \sim 10^4$ ), however, its pass from an inlet pipe to channels that are one or two orders of magnitude smaller, decreases the Reynolds number dramatically. Although, there is a strong reduction of the Reynolds, to the order of  $10^2$  typically, turbulence is still strong in the entry region. In these cases, laminar flow does not apply, also, correlations for turbulent flow are not meant to work at such low Reynolds numbers, neither for decaying turbulence. Clearly the decaying turbulence will affect the mass and heat transfer coefficients in the entry region, which could have a significant impact on the performance of the entire reactor; hence, it must be described accurately.

The goal of this study is to identify and quantify the effect of the decaying turbulence on the Nusselt along the entry region of monolith channels. We used circular channels as a first approach, which are still not studied under the mentioned conditions. Given the difficulty to measure accurate profiles inside channels of about 1 mm of diameter [4], the study used Large Eddy Simulation, which is a highly precise and extensively validated numerical technique, suitable for flows in transition. The results agreed previously reported data [1, 5], also showed a significant effect of the entering turbulence on the Nusselt along the beginning of the channels. This work extends available models for laminar flow, to take into account the turbulence. The proposed model describes the heat transfer in the transitional region accurately; it also converges to the correct Nusselt in the fully developed laminar zone. RANS models were also tested, finding different levels of agreement, but, in general, resulting not suitable to describe the entire region accurately.

## References

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