Theoretical Analysis of the Effect of Properties on the Solar Still Performance

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Abstract - Potable water not only is important for life but also for industrial and agricultural purposes. For many decades, the problem of water shortage has been one of the main challenges facing the world. Solar distillation is regarded by many investigators as one of the important methods to solve water scarcity problems. A solar still is a simple device which can be effectively used to convert saline water into fresh water. The productivity depends on many parameters, which among them are transmittance of the cover, thermal properties of the basin and water, and heat loss through the solar still. In this research, the effect of three design parameters (basin heat transfer coefficient, glass absorptivity and glass transmissivity) on performance of the conventional solar still was theoretically investigated and compared with experimental results. Iteration was necessary to obtain the values of the design parameters that produce good matching between the theoretical and experimental results. The effect of overall heat transfer coefficient \( U_b \) found to be significantly large especially at low values. It was found that reducing the overall heat transfer coefficient from 30 to 0.0 W/m² K will increase the production rate by 64.02%. It was also found that reducing the absorptivity from 0.1 to 0.01 will increase the production rate by 23.28%. The results showed that the solution is highly sensitive and depending on the precision of these parameters. It can be concluded that an accurate prior knowledge of these parameters is essential to obtain reasonable results. The experimental and theoretical hourly production rate are in good agreement at \( U_b = 5.9W/m^2K, \alpha_g = 0.075 \) and \( \tau_g = 0.845 \) where the maximum discrepancy between them is 23% at around 14:00.

Keywords: Productivity; Solar stills; Water desalination; Wick materials.

1. Introduction

The available amount of fresh water on earth is very limited, and the demands are significantly increased all over the world due to the rapid population growth and considerable increasing trends of agricultural and industrial requirements. Fresh water reserves are continually decreasing. Industrial wastes and sewage discharges have polluted reserves and underground water. The availability of clean and pure drinking water has become one of the most urgent needs for human community in many countries mainly in the Middle East and North Africa. The majority of areas that have deficiencies in fresh water supply have huge amounts of solar energy freely available [1,2]. A solar still is a simple device, which can be effectively used to convert saline water into fresh water. The enhancement of solar stills performance and improving their production capacity of distilled water are the main goals of the investigators in recent years [3]. The need for a small-scale solar distillation unit increases continuously, especially in arid regions where sunshine is abundant and fresh water is scarce. These devices are suitable for a single house or a small community for providing good quality of drinking water [4].

In order to have a clear idea about energy efficiency, it is convenient to study heat loss of the solar still. Thermal losses mainly occur through the glass cover by radiation and convection heat transfer to the ambient and through the bottom of the basin plate via the insulation by conduction and convection of heat transfer to the ambient. A prior knowledge of the outcome form solar still using theoretical model is of great importance to design and manufacture a solar still that meets the expectation in terms of functionality and productivity [5].

Ref. [6] reported a comprehensive study of heat transfer, mass transfer, and entropy rate of humid air for a single solar still. They concluded that minimum glass thickness and decreasing thermal losses of the solar still (mainly due to heat loss through the basin plate to the ambient) are the best operating parameters that give maximum solar still productivity. Ref. [7] studied the effect of parameters on the performance of solar stills. They found that productivity is largely affected by climatic, operational, and design parameters. Ref. [8] conducted a comprehensive energy analysis of a passive solar distillation system. Applying a set of typical design and operating parameters using a computer program,
the temperatures of basin-liner, saline water body and inner and outer glass cover are estimated. They found that a 100% increase in insulation thickness of the passive solar still will increase the energy efficiency and daily yield by 5.33% and 5.52%, respectively. Similar results were reported by Ref. [6]. Ref. [9] compared different mathematical models to describe the simultaneous heat and mass transfer process inside solar stills. The results of these models showed a wide range of discrepancy for the estimation of the daily productivity and thermal efficiency of the solar still. Ref. [10] tabulated the simulation parameters used in their model such as transmissivity, emissivity, absorptivity, specific heat and density for the glass, water and basin plate and used as overall heat transfer coefficient of 14 W/m²K. The basin overall heat transfer coefficient used in various publications varied between 2.8 and 20 W/m²K. Although this parameter is of great importance in solar still, most of these works provided no justification or sufficient information with regard to insulation applied in their systems. Therefore, the physical and thermal properties of the insulation materials are important parameters in terms of the solution of theoretical model and so must be accurately known to guaranty reliable results. The transmittance and absorptance of a glass depend on the type and thickness of the glass in particular the angle that the incidence beam of light makes with the normal to the surface. Ref. [11] provided data for the absorption and transmission of thermal radiation by single and double glazed windows (with index of refraction n = 1.2). Ref. [12] studied the effect of glass thickness on performance of flat plate solar collectors for fruits drying. Their results showed that the change in glass thickness results into variation into collector efficiency. They concluded that the use of 4 mm glass thick improves the performance of air solar collector by 7.6% compared to 3, 5, and 6 mm and the 4 mm glass thickness gave optimal transmittance and convective losses, and hence is the best glazing thickness.

The theoretical modeling is necessary in engineering field. It enables researchers easily, relatively and without essential expenses to investigate the properties and behavior of a system in any conceivable situation. A prior knowledge of the outcome form solar still using theoretical model is of great importance to design and manufacture a solar still that meets the expectation in terms of functionality and productivity. The present work is a theoretical study applied to solar stills to address the importance of the above-mentioned transmissivity, absorptivity, reflectance and the basin overall heat transfer coefficient and investigate their effect on the performance of the solar still.

2. THEORETICAL MODELING OF SOLAR STILL
2.1 Principles of Solar Still

Solar radiation is partially reflected to the outside and partially absorbed by the glass cover and mostly it is transmitted through the glass cover to the water in the basin. The water in turn absorbs small portion of the received solar radiation and transmit the rest to the basin in conventional solar stills. The solar radiation absorbed by water and the heat gain by the water from the basin will raise the water temperature above that of the glass cover. This allows the evaporated water to condense on the glass cover surface. Inside the solar still the increase in water temperature causes the vapor pressure at the air water interface to increase above that in the bulk of the air. Thus, the water evaporates as a result of the vapor pressure difference and the air humidity in the tank rise and so its dew point. Since the glass cover temperature is lower than the dew point of the humid air, condensation occurs on the glass surface. The evaporated water must be compensated to keep the water level in the tank [13-15].

![Energy transport mechanism in conventional solar still](image)
2. 2. Thermal Analysis of the Solar Still

In this work, the model of Ref. [16] who used a time dependent energy balance on solar stills, which will be modified modified to fit the current work conditions. The theoretical model will be using the measured data of the solar intensity, intensity, ambient temperature and wind speed given in Ref. [17]. The solution will be conducted at various absorptivity, absorptivity, transmissivity and basin overall heat transfer coefficient. The operation of solar still is governed by the various heat and mass transfer modes occurring in the system. The major energy transport mechanism in the still is shown in figure 1. Applying the conservation of energy to the conventional solar still components, namely the glass cover, saline water and basin, the following three equations are obtained.

Energy gained by the glass cover (from sun and convective, radiative and evaporative heat transfer from water to glass) is equal to the summation of energy lost by radiative and convective heat transfer between glass and sky, and energy stored by glass.

\[
I(t)A_g a_g + Q_{c.w-g} + Q_{r.w-g} + Q_{e.w-g} = m_g C_p g \left( \frac{dT_g}{dt} \right) + Q_g + Q_{c.g-sky}
\]

(1)

Energy received by the saline water in the still (from sun and base) is equal to the summation of energy lost by (1) convective heat transfer between water and glass, plus (2) the energy by the replaced cooler water that replaces the evaporated portion, (3) side wall loss and (4) energy stored by the saline water. The water reflectance is negligibly small.

\[
I(t)A_w a_w + Q_{c.bw} = m_w C_p w \left( \frac{dT_w}{dt} \right) + Q_{c.w-g} + Q_{r.w-g} + Q_{e.w-g} + Q_{f.w} + Q_{sw.loss}
\]

(2)

Energy received by the basin (from sun) is equal to the summation of energy (1) lost by convective heat transfer between basin and water, (2) heat lost from the bottom of the basin and (3) energy stored by the basin. It is assumed that all solar radiation reached the basin are absorbed by the basin with zero reflectance.

\[
I(t)A_b a_b = m_b C_p b \left( \frac{dT_b}{dt} \right) + Q_{c.bw} + Q_{b.loss}
\]

(3)

Where: \(a_g = \alpha_g (1 - r_g)\); \(a_w = \alpha_w \tau_g (1 - r_g)\); \(a_b = \alpha_b \tau_g \tau_w (1 - r_g)\).

(4)

(5)

(6)

(7)

(8)

(9)

(10)

(11)

Heat transfer between water and the glass cover:

- convective heat transfer coefficient is

\[
h_{c.wg} = 0.884 \left\{ \left( T_w - T_g \right) + \frac{(P_w - P_g)(T_w + 273.15)}{(286.9 \times 10^3 - P_w)} \right\}^{1/3}
\]

(13)

The radiative heat transfers is

\[
Q_{r.wg} = h_{r.wg} A_w (T_w - T_g)
\]

(14)

Where the radiative heat transfer coefficient is

\[
h_{r.wg} = \varepsilon \sigma \left[ (T_w + 273.15)^2 + (T_g + 273.15)^2 \right] (T_w + T_g + 546)
\]

(15)
form the comparison, the model was solved under 

\[ Q_{e,w,g} = h_{e,w,g} A_w (T_w - T_g) \]  

(17)

Where the evaporative heat transfer coefficient is 

\[ h_{e,w,g} = (16.273 \times 10^{-3}) h_{c,w,g} (P_w - P_g) / (T_w - T_g) \]  

(18)

The radiative heat transfers between sky and the glass is 

\[ Q_{r,g-sky} = h_{r,g-sky} A_g (T_g - T_{sky}) \]  

(19)

The radiative heat transfer coefficient is 

\[ h_{r,g-sky} = \epsilon \sigma [(T'_w)^4 + (T'_g)^4] (T_g + T_{sky}) \]  

(20)

where \( T'_w = T_w + 273 \) and \( T'_g = T_g + 273 \)

The effective sky temperature is \([16, 18]\)

\[ T_{sky} = T_a - 6 \]  

(21)

The convective heat transfers between sky and the glass is 

\[ Q_{c,g-sky} = h_{c,g-sky} A_g (T_g - T_{sky}) \]  

(22)

\[ h_{c,g-sky} = 2.8 + 3.0 V \]  

(23)

Where \( V \) is the wind velocity

2. 3. Bottom and sidewall heat transfer coefficients;

Since the solar still contents (basin plate, water and moist air) are at a higher temperatures than the outside ambient temperatures. A heat loss is expected to occur. Therefore the bottom and side wall are insulated. If the insulation is properly applied, the insulation thermal resistance will be the dominant one to other thermal resistances such the inside convective and radiative. However all thermal resistance may be included. The overall heat transfer coefficient of bottom heat loss is obtained as

\[ U_b = 1 / \left( \frac{1}{h_a} + \frac{x_{pw}}{k_{pw}} + \frac{x_{in}}{k_{in}} + \frac{x_s}{k_s} \right) \]  

(24)

Where in the thermal resistance of the insulation \((\frac{x_{in}}{k_{in}})\) is dominant. And the side wall overall heat transfer coefficient is approximated by researcher \([9, 19, 20]\) as

\[ U_{sw} = U_b \frac{A_{sw}}{A_b} \]  

(25)

Some researchers embedded the side heat transfer coefficient in the \( U_b \). In this case a value of 14 \( W/m^2 K \) \([15]\) and 20 \( W/m^2 K \)\([7]\) were used. Ref. \([21]\) took the side wall heat transfer coefficient as 0.5 \( W/m^2 K \). In this current work the side wall heat loss is obtained as

\[ U_{sw} = 1 / \left( \frac{1}{h_a} + \frac{x_{pw}}{k_{pw}} + \frac{x_{in}}{k_{in}} + \frac{x_s}{k_s} + \frac{1}{h_{cw} + h_{rw}} \right) \]  

(26)

Where \( h_{cw} = h_{c,w,g} \) and \( h_{rw} = h_{r,w,g} \). These coefficients are time dependent

3. RESULTS AND DISCUSSIONS

In this research, the effect of the three design parameters on performance of the conventional solar still has been theoretically investigated. These design parameters are basin heat transfer coefficient, glass absorptivity and glass transmiss [5]. To perform the comparison, the model was solved under similar condition as the one used in the experimental study. Other parameters used in this model are shown in table 1. From the current theoretical model the hourly production, the accumulated rate production, and the saline water, basin and glass temperatures are calculated and compared with the experimental results (Fig. 2–Fig. 8). This is done iteratively to find the applicable values of basin heat transfer coefficient, glass absorptivity and glass transmissivity. The analysis showed that (see Fig. 2) the experimental and theoretical accumulated production rate are in very good agreement at \( U_b = 5.9 W/m^2 K, \alpha_g = 0.075 \) and \( \tau_g = 0.845 \) except around 11:00 a.m. where it shows a discrepancy of 30%. Whereas the hourly production shows a good agreement with a maximum discrepancy of 23%. At the same conditions, the temperature deviation between theoretical and experiment is by 9.086% for saline water temperature 14.44% for basin temperature and 18.48 % for the glass temperature. As an essential part of the current work, the effect of the
three design parameters on the solar still performance is studied. During a design process, a theoretical model that predicts the solar still performance accurately plays a vital role. Thus, knowing the accurate values of these design parameters in advance will result in a better solar still design. Fig. 2-6 shows the effect of the basin heat transfer coefficient on the production and saline water, basin and glass temperatures. Ideally, a solar still must be perfectly insulated and so $U_b = 0$, which produces the highest accumulated production. An actual solar will always have some basin heat loss depending on the insulation material and installation. Compared with ideal insulated solar still, a $U_b$ of 5.9, 10, 20 and 30 $W/m^2 K$, the accumulated production drops by 37.17%, 47.02 %, 58.53 and 64.02% respectively. The slope of the drop in production is steeper at low $U_b$ (Fig. 9) at which the system must be designed. For example if the $U_b = 1 W/m^2 K$, the drop will 10.64% which is significantly large. Similarly, the effect of $U_b$’s on the saline water, basin and glass temperatures is significantly large at low $U_b$’s. The temperatures drops with increasing $U_b$’s (see Fig. 4-5). Based on average values, the deviation from the perfect insulated solar still for $U_b$ of 5.9, 10, 20 and 30 $W/m^2 K$ for the saline water is 14.51 %, 18.015% and 24.94% respectively whereas for the basin the drop in temperature is 9.982%, 14.0% 19.32%, and 22.18% and for the glass temperature is 25.77%, 28.88%, 32.75% and 34.71% respectively.

The effect of the glass absorptivity and transmissivity is also studied. The glass reflectance was taken as 0.08 for glass thickness up to 5 mm [22]. Therefore the tradeoff is then between the absorptivity and transmissivity so the sum of the three is always one. From Fig. 7 and 8, the effect of these parameters is obvious. By reducing the glass absorptivity (i.e. increasing the glass transmissivity), the production rate increases due to the fact more solar radiation are passing to the basin. It is essential to use a glass with a low absorptivity in solar still to have high performance. At the same time, it is of great importance to incorporate in the theoretical model accurate values for these parameters in order to produce trustful results. This can be seen from the significant drop in the accumulated production for the absorptivity range of 0.01-0.1 (calculated based on the production at 0.01absorptivity). This drop in accumulated production for absorptivity of 0.025, 0.05, 0.075, and 0.1 is 4.0%, 10.63 %, 17.04 and 23.28% respectively.

The effect of basin overall heat transfer coefficient on hourly production rate.

$$\alpha_g = 0.075, \tau_g = 0.845$$

4. CONCLUSIONS

Generally to develop a mathematical model it is required to know the basic design parameters such as the four basic properties that affect radiant energy transfer: transmittance, reflectance, absorptance, and emittance as well as all the external parameters such as the insulation characteristic, which dominate the overall heat transfer coefficient. Previous research using mathematical modeling either gave the values of these parameters without justification and reference or provided
no clue of what values they used to obtain their results. This study is an attempt to predict production rate of the conventional solar still. In this research, the effect of the three design parameters ($U_b$, $\alpha_g$ and $\tau_g$) on performance of the solar still has been theoretically investigated and compared to the experimental results. Iteration was necessary to obtain the values of the design parameters that produce good matching with the experimental which were $U_b = 5.9$ $W/m^2 K$, $\alpha_g = 0.075$ and $\tau_g = 0.845$. The effect of $U_b$ found to be significantly large especially at low $U_b$. Compared to ideally perfectly insulated solar still, i.e. increasing $U_b$ up 30 $W/m^2 K$, the accumulated production drops by 64.02% respectively. Similarly the effect of $U_b$'s on the temperatures is significantly large at low $U_b$'s. Based on average values, the deviation from the perfect insulated solar still for example increasing $U_b$ up to 30 $W/m^2 K$ for the saline water is 24.94% whereas for the basin the drop in temperature is 22.18% and for the glass temperature is 34.71% respectively. The effect of the $\alpha_g$ and $\tau_g$ is also studied. By reducing $\alpha_g$ (i.e. increasing $\tau_g$) the production rate increases due to the fact that more solar radiation are passing to the basin. It is essential to have a glass cover with low absorptivity in solar still to have high performance. The larger the absorptivity, the more significant the drop in the accumulated production. This drop for absorptivity of 0.025, 0.05, 0.075, and 0.1 is 4.0%, 10.63 %, 17.04 and 23.28% respectively.
**NOMENCLATURES**

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<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
<th>Unit</th>
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<tr>
<td>(A)</td>
<td>area</td>
<td>([m^2])</td>
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<tr>
<td>(C)</td>
<td>specific heat</td>
<td>([J/kg,K])</td>
</tr>
<tr>
<td>(h)</td>
<td>heat transfer coefficient</td>
<td>([W/m^2,K])</td>
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<tr>
<td>(h_{fg})</td>
<td>enthalpy of evaporation at Tw</td>
<td>([J/kg])</td>
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<tr>
<td>(I(t))</td>
<td>intensity of solar radiation</td>
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<tr>
<td>(m)</td>
<td>mass</td>
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<tr>
<td>(P)</td>
<td>partial pressure</td>
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<td>(Q)</td>
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<td>(U)</td>
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<td>(V)</td>
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<td>(x)</td>
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**Greeks**

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<td>(\epsilon)</td>
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<tr>
<td>(\rho)</td>
<td>density, ((kg/m^3))</td>
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<td>(\tau)</td>
<td>transmissivity</td>
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**Subscripts**

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<td>radiation</td>
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<tr>
<td>(s)</td>
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**Fig. 8:** effect of Absorptivity and transmissivity on hourly production rate. \(U_b = 5.9\, W/m^2\,K\), reflectivity factor = 0.08

**Fig. 9:** the accumulated production, saline water, basin and glass temperatures versus the basin heat transfer coefficient. \(a_g = 0.075, \tau_g = 0.845\), reflectivity factor = 0.08