

Human Upper Limb Mass-Inertial Characteristics via Computer Modelling

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Abstract - We present a new modified biomechanical geometrical model of human upper limb, with the help of three-dimensional geometrical mathematical modelling – 3D (GMM). This model represents a modification of the ones suggested in [1, 2, 3, 4] and is based on our own anthropometric measurements of 50 men aged between 30–40 years. Using the model, we calculate the volume and mass, the center of mass and the principal moments of inertia for the human body upper limb for two basic sub-cases: *i*) determination of these parameters for the separate parts of the upper limb: upper arm, lower arm and hand and *ii*) for the human upper limb as a whole. For the last we used the computer realization of the model. In order to validate the accuracy of the program we have performed a detailed comparison of the numerical results obtained within the program with the numerical evaluation of the analytical expressions that we have derived for the corresponding quantities. We observed an excellent agreement between the two approaches. Finally, we also present a comparison between the results obtained within our model with data for other Caucasian reported in literature. We observe an overall good agreement among all of them with the data gained for Bulgarian males. The proposed model is oriented to application in medicine (orthopedics and traumatology) and engineering when designing devices aimed to help disabled individuals. It can predict data for the inertial parameters of a given male individual provided the corresponding easily measurable geometrical data for this individual are known.

Keywords: Biomechanics, mass moments of inertia, human upper limb model, three-dimensional geometrical mathematical modelling – 3D (GMM), manipulation system, body segment parameters, mass-inertial characteristics, mass properties

1. Introduction

The investigation on the human body geometric and mass-inertial characteristics is of key importance in human motion analysis. In our everyday activities – when working, driving a vehicle, even when taking a meal, or even drinking a water and not to speak about all possible sport activities the use of the limbs is crucial. The last is, obviously, to be taken into account when one needs to design a device for supporting an impaired person in any of these activities and to provide, as good as possible, the quality of life for such an individual. We are going to study the mass-inertial characteristics of a male person with the help of mathematical and computer modeling. When doing that, one has to resolve a set of problems. They include: 1) the proper segmentation of the limb; 2) the choice of the anthropometric points used to defined these segments; 3) the set of geometrical data characterizing the so defined segments; 4) the choice of geometrical figures with the help of which the segments are to be modeled; 5) determination of the needed geometrical characteristic pertinent for this geometrical bodies based on the measured data; 6) derivation of mathematical expressions for any of the characteristics of interest; 7) numerical evaluation of these expressions using experimentally available data for the additional information needed, say, the density of the corresponding segment; 8) computer realization of the mathematical model in the framework of a suitable software package; 9) validation of the computer model via comparison of the data obtained from the computer model with the data obtained from the analytical expressions; 10) obtaining data on the basis of the computer model for situations in which analytical results are missing or is elaborative to be derived; 11) comparison of the so derived data with the ones reported previously, when available, in the literature for persons belonging to the same or similar type.

In the current article we have realized the above program of points for the upper limb of an average Bulgarian male.

One of the earliest studies of mass, volume and center of mass of male cadavers are those of [5, 6]. In the 60-s and 70-s a number of studies have reported anthropometric and mass-inertial of the segments of the human body of elderly male cadavers [7, 8, 9]. Different methods for investigation of body segment mass-inertial parameters obtained for living male individuals have been used: immersion and cast method [10], gamma mass scanning [11], geometrical modeling [12, 13]. The approach utilized in the current study is based on geometrical modeling.

2. The Model and the Procedure

Let us now explain in a bit more details what we have actually done in order to achieve the goals outlined above aimed to determine the mass inertial parameters of the upper limb of the average Bulgarian male.

We start from the model proposed [1] in of the average Bulgarian man. In the current article, however, we improve the way how one models there the upper arm and the lower arm. Instead of considering them of using frustums of a cone, as in [1], we represent these parts of the upper limb with versions of right elliptical stadium solids (see Fig. 1). The modeling of hand (fist) remains the same as in [1, 2, 3]. Let us immediately stress that one of the consequences of modelling the upper and lower segments of the upper limb via right elliptical stadium solids is the lack of the “left-right” symmetry for the inertial moments of these segments. The last symmetry was preserved in [1] and is usually also present in most of the geometrical models of the human body we are aware about. In [1] the main part of the geometrical data needed to determine the geometrical parameters of the segments of the body is taken from a detailed representative anthropological investigation of the Bulgarian population [14] where the authors measured a total of 2435 males. Unfortunately, the data collected does not include all the data needed to model the upper and the lower arm as right elliptical solids. For that reason, we made our own complementary anthropometric measurements of these segments on additional 50 Bulgarian males.

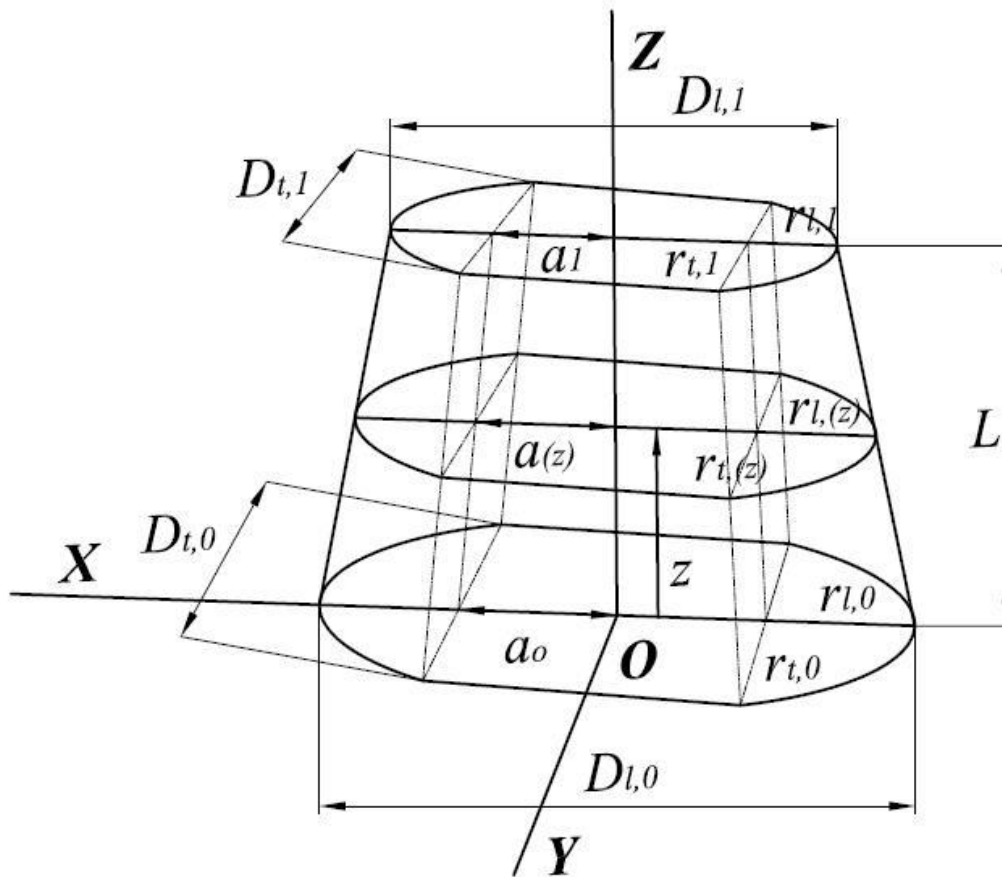


Fig. 1: A right elliptical stadium solid.

2.1. Description of the Data

In the anthropometric measurements, which we performed, data for D_l , D_t and L_{cir} (see Fig. 1) have been collected both for the upper and for the lower arm.

• For the upper arm, that extends between *acromion-radiale*, we measured the circumference across epicondyles (L_{cir}), the epicondilar diameter of humerus ($D_{l,0}$), the diameter perpendicular to humerus ($D_{t,0}$), as well as the axillary circumference at the proximal end. From these data the values of a_0 , a_l , $r_{l,0}$, $r_{l,l}$, $r_{y,0}$ and $r_{t,l}$ can be easily inferred: r_t directly follows from $r_t = D_t/2$, r_l can be determined by numerically solving the equation

$$L_{cir} - 2D_l = 4r_l \left[E \left(\sqrt{1 - \frac{r_t^2}{r_l^2}} \right) - 1 \right] \quad (1)$$

using r_t from above, and, finally, one has for $a = (D_t - 2r_t)/2$. The vertical lengths of the upper arm, as well as of all the other segments (L) are taken from [14].

• The lower arm is taken to be, as usual, between the points *radiale-stylian*. Obviously, the necessity of smooth tailoring demands that the parameters for its proximal end are the same as the above-mentioned dimensions for the distal end of the upper arm. For the wrist (distal end) of lower arm (see Fig. 1), but turned upside down), we measured breadth of radio-ulnar joint ($D_{l,l}$), the thickness in the middle of the radio-ulnar joint perpendicular to its breadth ($D_{t,l}$) and the radio-ulnar joint circumference (L_{cir}).

The average data for the directly measured independent geometrical parameters D_l , D_t and L_{cir} described above can be found in [3]. With the data measured for D_l , D_t and L_{cir} , and having in mind the analytical properties of the stadium solid, as explained above, one can determine the values of the parameters a , r_l and r_t characterizing the corresponding segments – the upper and the lower arm, correspondingly. The values, obtained in this way, are reported in Table 1. Let us remind that, as reported in [1, 2, 3], the height and weight of the average man are 1.71.m and 77.7 kg. In Table 1, in additions, the lengths L (in cm) of the segments according to [14], also the densities ρ (in kg/m^3) of the segments according to [15] are given.

Table 1: Calculated parameters (cm), lengths and densities (kg/m^3) for males.

SEGMENT	P A R A M E T E R S (see ref. [3])							
	a_0	$r_{l,0}$	$r_{t,0}$	a_l	$r_{l,l}$	$r_{t,l}$	L	ρ
UPPER ARM	3.7	0.3	3.0	4.5	0.3	3.7	30.9	1053
LOWER ARM	3.7	0.3	3.0	2.5	0.2	1.7	24.7	1100
SPHERE			$R_{HA} = 4.7$					

2.2. Comments on the Procedure

Using the original experimental data measured and the analytical properties of the solid bodies involved in modelling the segments of the human body, see, e.g., equations (2)–(4), we calculate the mass-inertial characteristics of the average Bulgarian man. We do that for any segment of the upper limb. We have derived analytical expression for the volume of the segments, their mass, the coordinates of the center of mass, and the principal moments of inertia. For simplicity of the exposition we avoid presenting all these quite lengthy expressions here. We have restricted ourselves to presenting the expressions for the principal moments of inertia for the upper arm and lower arm. The moments can be determined using equations (2)–(4).

$$\begin{aligned}
I_{XX} &= \frac{1}{240} L \rho \left\{ - \frac{10L^2 [\pi(r_{l,0} + r_{l,1})r_{t,0} + \pi(r_{l,0} + 3r_{l,1})r_{t,1} + 4a_0(r_{t,0} + r_{t,1}) + 4a_1(r_{t,0} + 3r_{t,1})]^2}{r_{t,0}[8a_0 + 4a_1 + \pi(2r_{l,0} + r_{l,1})] + r_{t,1}[4a_0 + 8a_1 + \pi(r_{l,0} + 2r_{l,1})]} \right. \\
&+ 16a_0 [4r_{t,0}^3 + 3r_{t,0}^2 r_{t,1} + 2r_{t,0} r_{t,1}^2 + r_{t,1}^3 + L^2(2r_{t,0} + 3r_{t,1})] \\
&+ 16a_1 [r_{t,0}^3 + 2r_{t,0}^2 r_{t,1} + 3r_{t,0} r_{t,1}^2 + 4r_{t,1}^3 + 3L^2(r_{t,0} + 4r_{t,1})] \\
&+ \pi [(3[(4r_{l,0} + r_{l,1})r_{t,0}^3 + (3r_{l,0} + 2r_{l,1})r_{t,0}^2 r_{t,1}] + (2r_{l,0} + 3r_{l,1})r_{t,0} r_{t,1}^2 + (r_{l,0} + 4r_{l,1})r_{t,1}^3] \\
&\left. + 4L^2(r_{l,0}(2r_{t,0} + 3r_{t,1}) + 3r_{l,1}(r_{t,0} + 4r_{t,1})) \right\}; \tag{2}
\end{aligned}$$

For the hand the expressions needed have been already derived and presented in [1].

$$\begin{aligned}
I_{YY} &= \frac{1}{720} L \rho \left\{ 48a_0^3(4r_{t,0} + r_{t,1}) + 48a_1^3(r_{t,0} + 4r_{t,1}) \right. \\
&+ 12a_0^2 \{ 3[4a_1 + \pi(4r_{l,0} + r_{l,1})]r_{t,0} + (8a_1 + 3\pi r_{l,0} + 2\pi r_{l,1})r_{t,1} \} \\
&- 30L^2 \frac{[(\pi(r_{l,0} + r_{l,1})r_{t,0} + \pi(r_{l,0} + 3r_{l,1})r_{t,1} + 4a_0(r_{t,0} + r_{t,1}) + 4a_1(r_{t,0} + 3r_{t,1}))]^2}{[8a_0 + 4a_1 + \pi(2r_{l,0} + r_{l,1})]r_{t,0} + [4a_0 + 8a_1 + \pi(r_{l,0} + 2r_{l,1})]r_{t,1}} \\
&+ 12a_1^2 \pi [r_{l,0}(2r_{t,0} + 3r_{t,1}) + 3r_{l,1}(r_{t,0} + 4r_{t,1})] \\
&+ 16a_1 [4r_{l,0}r_{l,1}(2r_{t,0} + 3r_{t,1}) + 9L^2(r_{t,0} + 4r_{t,1}) + 6r_{l,1}^2(r_{t,0} + 4r_{t,1}) + r_{l,0}^2(6r_{t,0} + 4r_{t,1})] \\
&+ 8a_0 [8(6r_{l,0}^2 + 3r_{l,0}r_{l,1} + r_{l,1}^2)r_{t,0} + 4(3r_{l,0}^2 + 4r_{l,0}r_{l,1} + 3r_{l,1}^2)r_{t,1} + 6a_1^2(2r_{t,0} + 3r_{t,1})] \\
&+ 6L^2(2r_{t,0} + 3r_{t,1}) + 3\pi a_1 (3r_{l,0}r_{t,0} + 2r_{l,1}r_{t,0} + 2r_{l,0}r_{t,1} + 3r_{l,1}r_{t,1}) \\
&+ 3\pi \{ 3r_{l,0}^3(4r_{t,0} + r_{t,1}) + 3r_{l,0}r_{l,1}^2(2r_{t,0} + 3r_{t,1}) + 3r_{l,1}^3(r_{t,0} + 4r_{t,1}) + r_{l,1}r_{l,0}^2(9r_{t,0} + 6r_{t,1}) \\
&\left. + 4L^2[r_{l,0}(2r_{t,0} + 3r_{t,1}) + 3r_{l,1}(r_{t,0} + 4r_{t,1})] \right\} \tag{3}
\end{aligned}$$

$$\begin{aligned}
I_{ZZ} &= \frac{1}{720} L \rho \left\{ 48a_0^3(4r_{t,0} + r_{t,1}) + 48a_1^3(r_{t,0} + 4r_{t,1}) \right. \\
&+ 12a_0^2 \{ 3[(4a_1 + \pi(4r_{l,0} + r_{l,1}))r_{t,0} + (8a_1 + 3\pi r_{l,0} + 2\pi r_{l,1})r_{t,1}] + (4r_{l,0})^3 \\
&+ 9\pi \{ r_{t,0} [4r_{l,0}^3 + 3r_{l,1}r_{l,0}^2 + 2r_{l,0}r_{l,1}^2 + r_{l,1}^3 + (r_{t,1} + 4r_{l,0})r_{t,0}^2] \\
&+ [r_{l,0}^3 + 2r_{l,1}r_{l,0}^2 + 3r_{l,0}(r_{l,1}^2 + r_{t,0}^2) + 2r_{l,1}(2r_{l,1}^2 + r_{t,0}^2)]r_{t,1} \\
&+ (2r_{l,0} + 3r_{l,1})r_{t,1}^2 r_{t,0} + (r_{l,0} + 4r_{l,1})r_{t,1}^3 \} \\
&+ 12a_1^2 \pi [r_{l,0}(2r_{t,0} + 3r_{t,1}) + 3r_{l,1}(r_{t,0} + 4r_{t,1})] \\
&+ 8a_0 [8r_{t,0}(6r_{l,0}^2 + 3r_{l,0}r_{l,1} + r_{l,1}^2 + 3r_{t,0}^2) + 2(6r_{l,0}^2 + 8r_{l,0}r_{l,1} + 6r_{l,1}^2 + 9r_{t,0}^2)r_{t,1} \\
&+ 12r_{t,0}r_{t,1}^2 + 6r_{t,1}^3 + 6a_1^2(2r_{t,0} + 3r_{t,1}) \\
&+ 3\pi a_1 (3r_{l,0}r_{t,0} + 2r_{l,1}r_{t,0} + 2r_{l,0}r_{t,1} + 3r_{l,1}r_{t,1})] \\
&+ 16a_1 [4r_{l,0}r_{l,1}(2r_{t,0} + 3r_{t,1}) + r_{l,0}^2(6r_{t,0} + 4r_{t,1}) \\
&\left. + 3[r_{t,0}^3 + 2r_{t,0}^2 r_{t,1} + 3r_{t,1}^2 r_{t,0} + 4r_{t,1}^3 + 2r_{l,1}^2(r_{t,0} + 4r_{t,1})] \right\}. \tag{4}
\end{aligned}$$

In the current study, based on the model, we provide data for the mass-inertial parameters of the male upper limb and compare our results with those available from the literature. In order to do that, for the whole upper limb we use a realization of the model within a CAD system - SolidWorks. The computer-generated model has been carefully verified.

Table 2: Moments of inertia of the body segments through the center of mass ($\text{kg}\cdot\text{cm}^2$) for males, compared with the already performed analytical analysis.

SEGMENT	ANALYTICAL CALCULATIONS			PRESENT DATA using 3D (GMM)		
	Ixx	Iyy	Izz	Ixx	Iyy	Izz
UPPER ARM	156.466	161.414	19.1882	156.47462	161.42413	19.19043
LOWER ARM	42.8028	44.4078	5.05819	42.81349	44.42104	5.06232
HAND	4.37	4.37	4.37	4.3691	4.3691	4.3691

We have compared the data obtained within the computer model with those derived from the analytical results for the segment. We have found excellent agreement between these data for the different segments of the upper limb. The program reproduces segment-by-segment data about volume, mass, center of mass and moments of inertia – see Table 2. That gives us confidence that this model could be used to calculate these characteristics for the whole upper limb. After determining them on the basis of the computer model, we compared our model results with the results available in literature for mass, volume and center of mass of the whole human upper limb for persons belonging to the same or similar type. The data are given in Tables 3, 4 and 5, respectively. The inspection shows a reasonably good agreement between our results and those previously reported in the literature. Data for the moments of inertia of the whole upper limb are reported in Table 6. The authors are not aware of other such data for the moments of inertia of the upper limb - almost all data available in the literature are for different segments, not for limbs as a whole. A visualization of the principal CAD model realization of the human upper limb within the SolidWorks media is shown in Fig. 2.

Table 3: Mass of the whole male's upper limb (kg).

	Min	Max	Mean
Braune and Fisher (right)	3.52	4.95	4.01
Braune and Fisher(left)	3.48	4.79	3.99
Chandler et al.(right)	2.65	4.42	3.36
Chandler et al.(left)	2.71	4.32	3.35
Clauser et al.	2.65	4.18	3.22
Dempster (right)	2.12	3.95	2.97
Dempster (left)	2.13	3.89	2.87
Drillis and Contini	-	-	4.38
Harless (right)	2.63	4.47	3.39
Harless (left)	2.45	3.77	2.94
Zatsiorsky and Seluyanov	-	-	3.60
Our data	-	-	3.25

Table 4: Volume of the whole male's upper limb (10^{-3}m^3).

	Min	Max	Mean
Chandler et al.(right)	2.60	4.36	3.28
Chandler et al.(left)	2.63	4.27	3.25
Clauser et al.	2.38	3.96	2.98
Drillis and Contini	3.51	4.58	3.97
Harless (right)	2.40	4.09	3.25
Harless (left)	2.22	2.39	2.31
Our data	-	-	3.02

Table 5: Location of the center of mass of the whole male's upper limb measured from the proximal end (cm).

	Min	Max	Mean
Chandler et al.	29.2	37.7	32.0
Drillis and Contini	-	-	25.3
Our data	-	-	28.5

Table 6: Predicted moments of inertia of the body segments through the center of mass ($\text{kg}\cdot\text{cm}^2$) for males. The data are obtained by 3D-GMM computer analysis.

Assembly	Ixx	Iyy	Izz
Upper + lower arm	62.670388	63.326094	24.25276
Upper + lower arm + hand	1220.06762	1226.62468	28.62192

The calculation procedure of 3D GMM is oriented to application in medicine (orthopaedics and traumatology, orthotics and prosthesis design), anthropomorphic and rehabilitation robotics, ergonomics, sport, etc. The proposed model can predict data for the inertial parameters of a given male individual provided, if the corresponding easily measurable geometrical data for this particular individual are known.

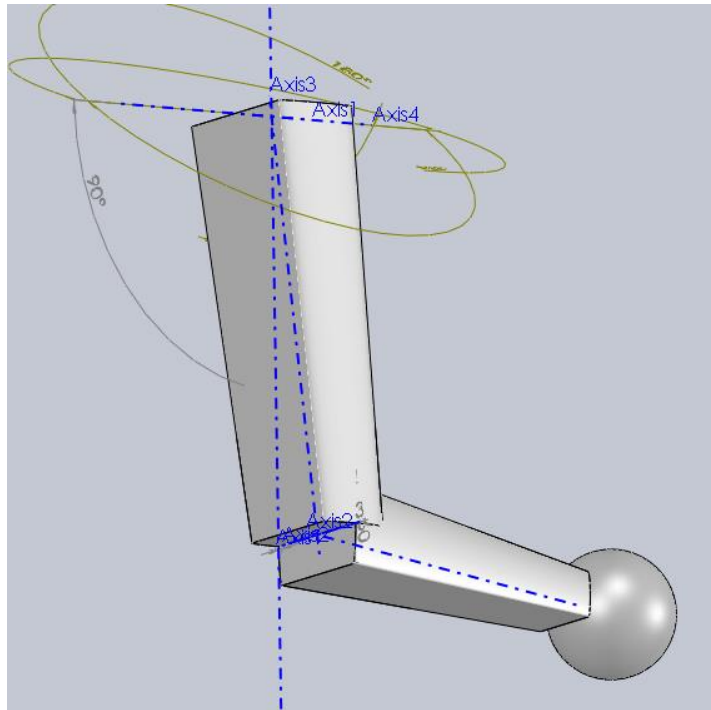


Fig. 2: SolidWorks media realization of the human upper limb model.

The computer generated model allows also to study the mass-inertial characteristics of the upper limb in any reasonable position and, thus, to study dynamics, and to predict characteristics which devices aimed to help a disabled person shall have in order to assist in performing a given specific motion.

3. Conclusions

In this paper, a new approach for determination of the human upper limb mass-inertial characteristics is presented by using the 3D geometrical mathematical modelling analysis approach. These results, as compared with the analytically calculates ones, demonstrate a very good concord with each other. There is also a good agreement with previously published data in the available literature. That is why authors believe that the presented approach is a qualitative

contribution to the technique of determination of the mass moments of inertia, presented so far, that can be in addition reliably and with confidence used to determine the mass inertial characteristics of the whole upper limb and to study different position of the limb, as well as its dynamics, etc.

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